

# Meta-learning using privileged information for dynamics

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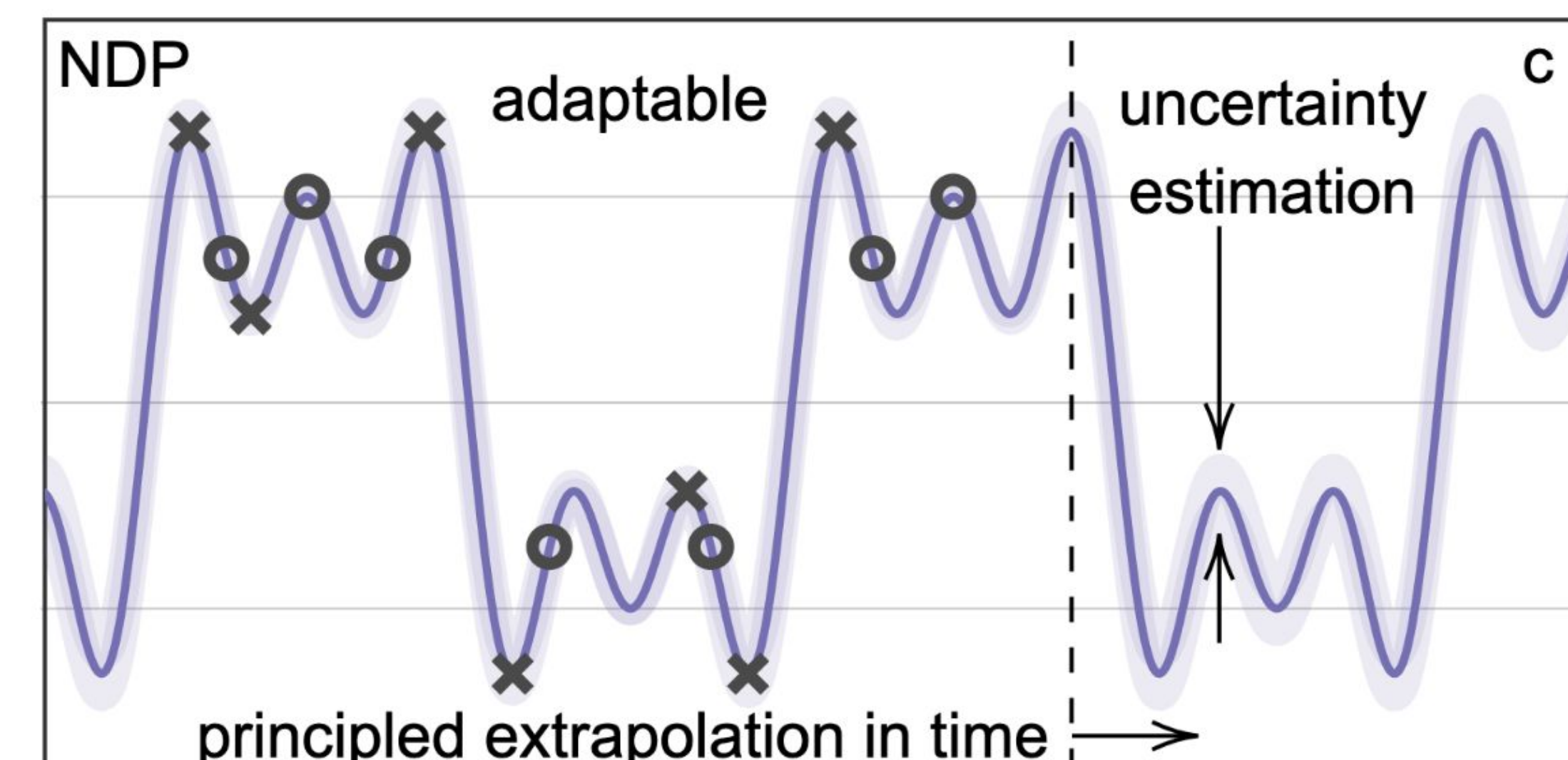
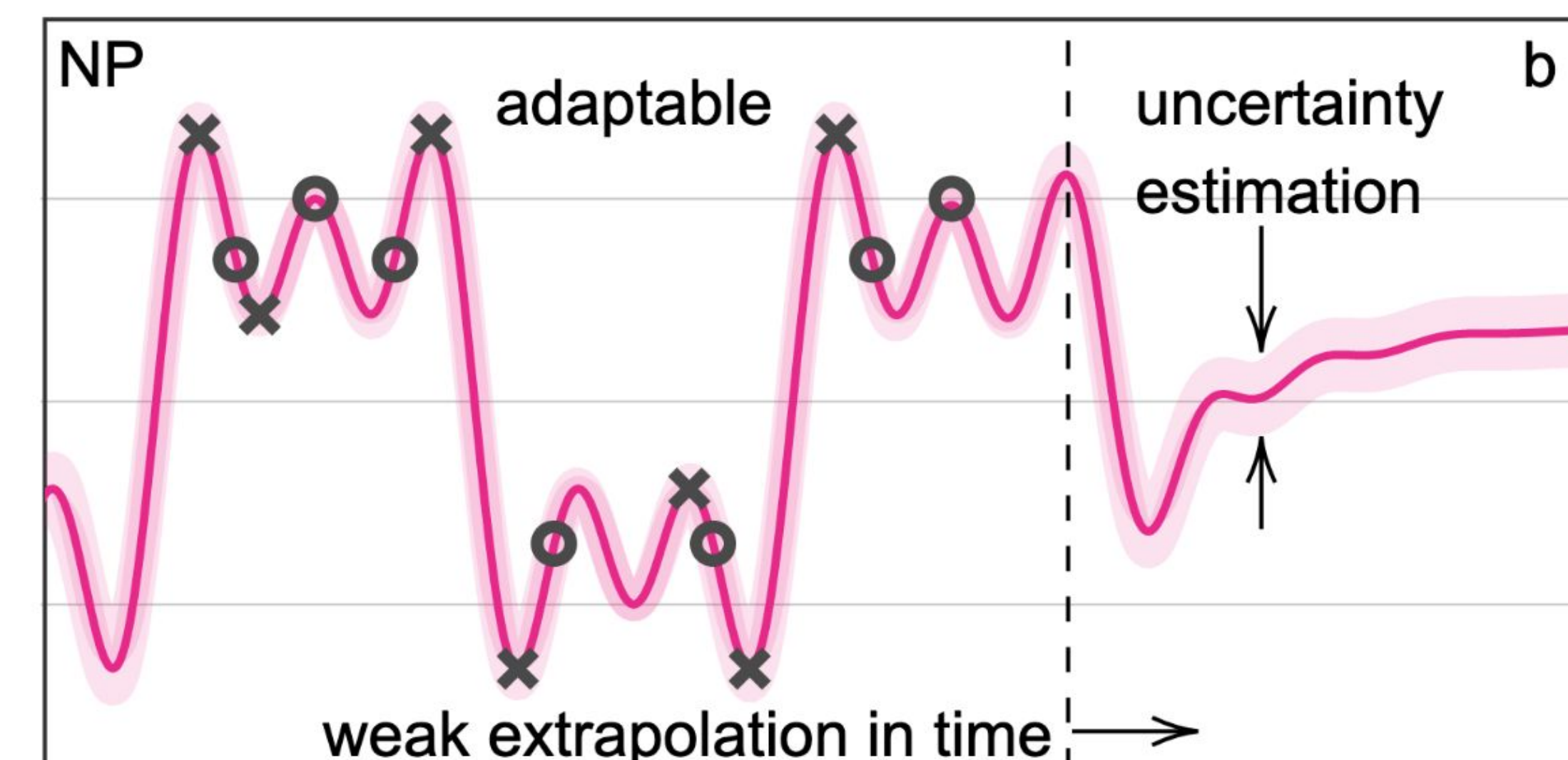
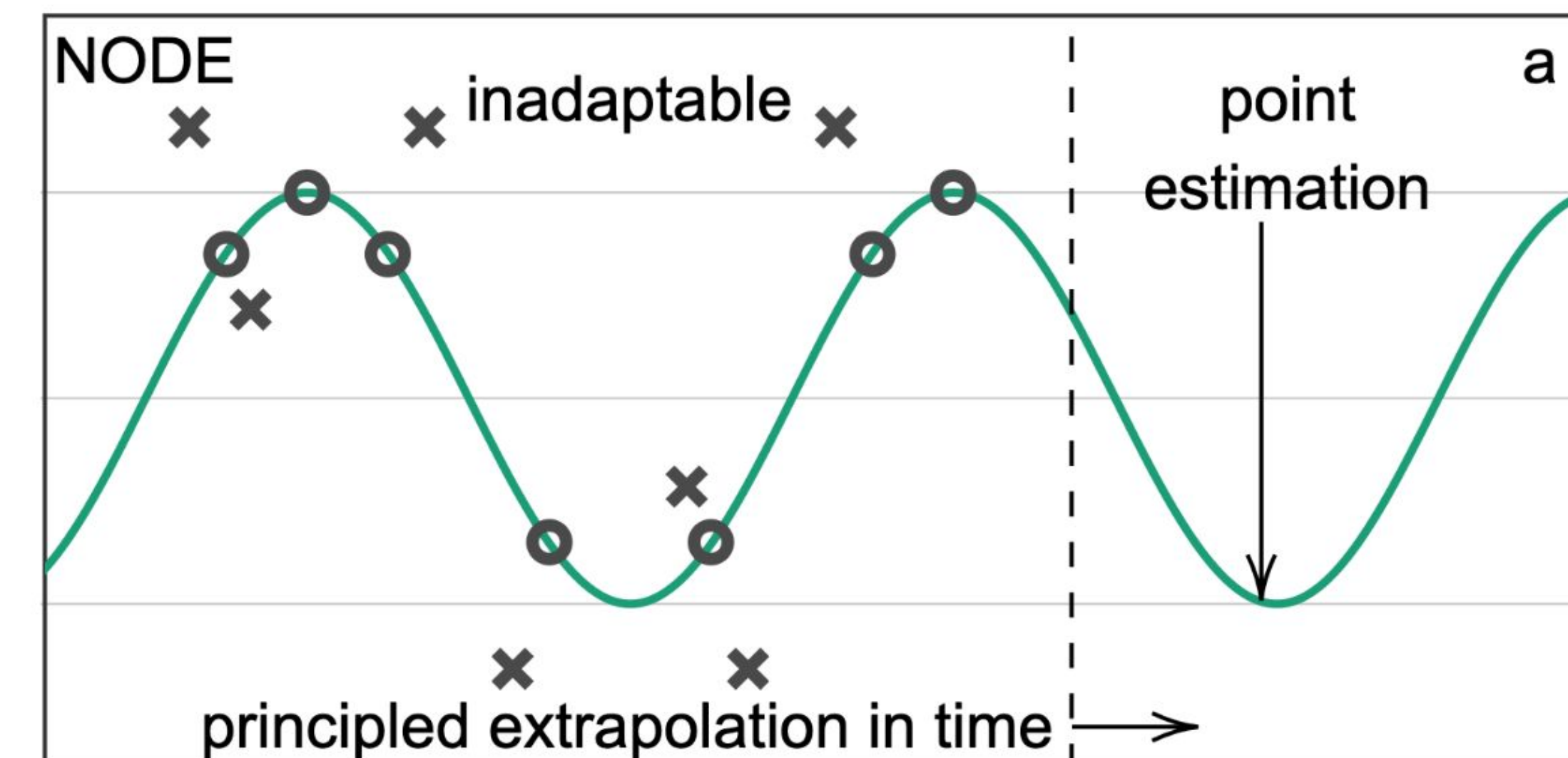
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Code: [github.com/bjd39/lupi-ndp](https://github.com/bjd39/lupi-ndp)

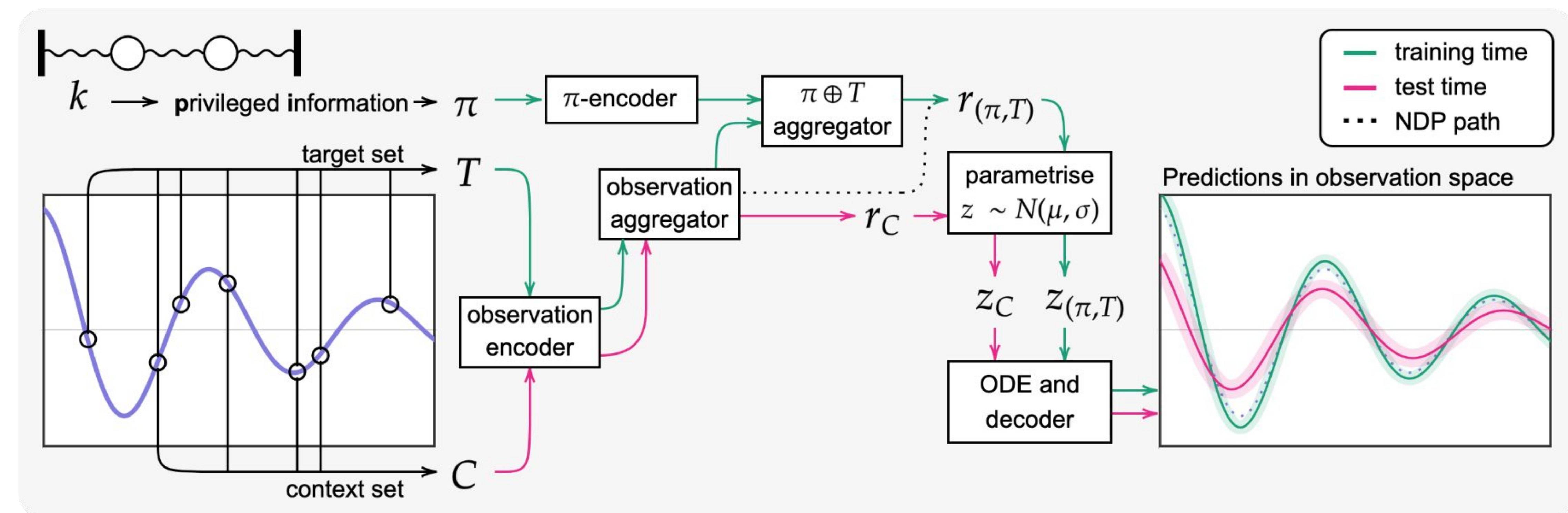
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**Background:** Neural ODEs (NODE), NPs, and NDPs



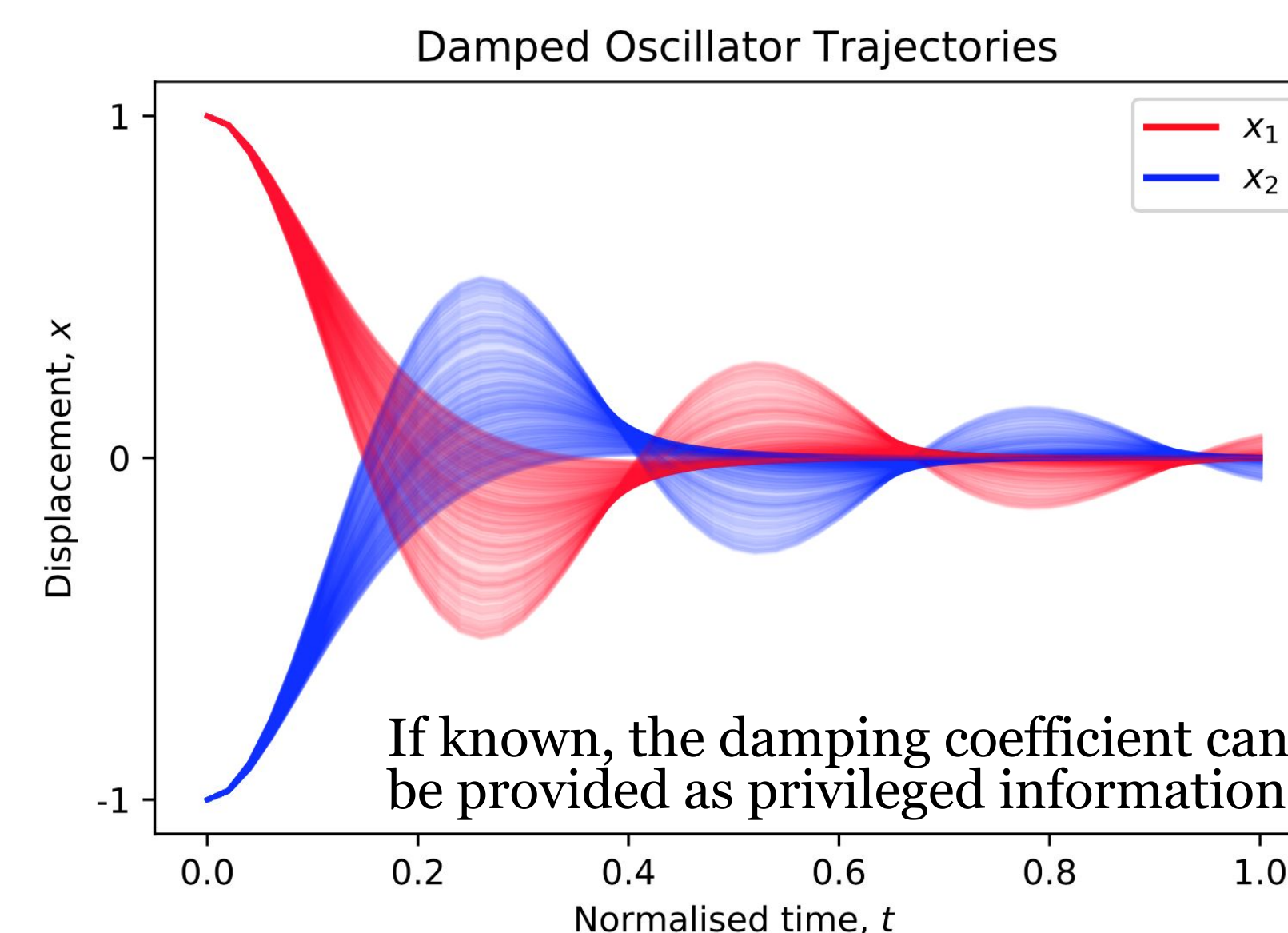
○ training observations; × test time additional context

**tl;dr:** Can we better meta-learn dynamics if we have access to high-level descriptions at training time? (Yes.)



**1.** Neural ODE Processes (NDP) approach meta-learning dynamics with a latent variable model, and inherit a flexible context aggregation mechanism from the Neural Process (NP): arbitrarily sized sets of observations are aggregated into a fixed length representation. **2.** In the sciences, we often have access to high-level information in addition to observations (e.g. known conserved quantities) this is *privileged information*.

→ Taking advantage of the aggregation flexibility, we extend NDPs to use additional information within the Learning Using Privileged Information (LUPI) setting (training only) and find general improvements.



Model	Varying stiffness, $k \sim U(0.2, 1)$			Varying damping, $c \sim U(0.5, 2)$		
	MSE ↓	Calib. error ↓	Sharp. ↓	MSE ↓	Calib. error ↓	Sharp. ↓
NoPI	1.05 ± 0.05	0.51 ± 0.02	6.88	2.82 ± 0.29	0.84 ± 0.04	2.15
LUPI	<b>0.93 ± 0.04</b>	<b>0.47 ± 0.02</b>	6.57	<b>2.39 ± 0.09</b>	<b>0.37 ± 0.02</b>	4.71
NoPI*	0.16 ± 0.02	2.69 ± 0.02	1.00	0.56 ± 0.02	1.56 ± 0.03	0.93
LUPI*	<b>0.06 ± 0.01</b>	<b>0.91 ± 0.02</b>	1.10	<b>0.25 ± 0.01</b>	<b>0.73 ± 0.03</b>	1.18

Model	L-V, $u_0 \sim U(0.2, 1), v_0 \sim U(0.1, 0.5)$		
	MSE ↓	Calib. error ↓	Sharp. ↓
NoPI	6.44 ± 0.44	2.19 ± 0.05	2.23
LUPI	<b>1.82 ± 0.13</b>	<b>0.90 ± 0.04</b>	3.44
NoPI*	5.24 ± 0.30	2.89 ± 0.04	1.37
LUPI*	<b>0.73 ± 0.02</b>	<b>1.23 ± 0.04</b>	1.48

\* indicates 'training mode' i.e. additional observations and privileged information provided